The solution of the following equation

$$\int_0^{\sum_{n=1}^{\infty} \frac{1}{n^2}} \frac{\prod_i (x+1)^i}{\sum_n \frac{1}{n^3}}$$

cannot be find easily. On the other hand, using an approximation one guesses